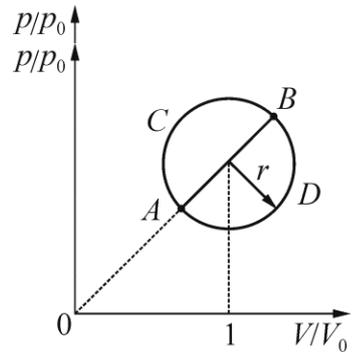


Theoretical Problems

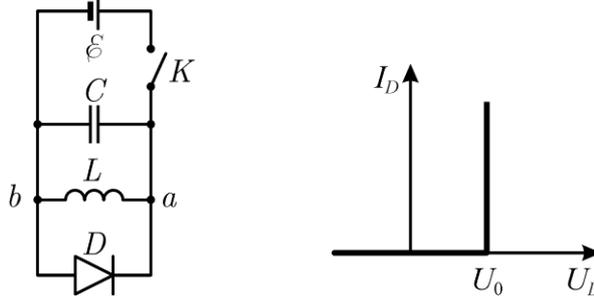
Problem 1

Two heat engines use an equal amount of ideal monatomic gas as a working substance. The PV diagram shows the engine thermodynamic cycles which combine into a single circle. The first engine cycle is represented by the semicircle $ACBA$ and the second engine cycle by the semicircle $ABDA$. The circle diameter AB lies on a straight line drawn through the origin. At ACB gas only receives heat from a source and at BDA only transfers heat to a sink. The circle centre is located at the point $(1,1)$ and the circle radius $r = 1/\sqrt{10}$. What is the ratio of the maximum efficiency of the second engine to the maximum efficiency of the first one?



Problem 2

The circuit on the left consists of an inductor L , a capacitor C , and a diode D which current-voltage characteristic is shown on the right (I_D is a current through the diode and $U_D = \phi_b - \phi_a$, where ϕ_a and ϕ_b are potentials at the corresponding points). All resistances including an internal resistance of the battery cell are negligible. Initially the switch K is opened and the capacitor C has no charge. Then the switch is closed for a period $t_0 \ll \sqrt{LC}$ and opened again. Determine a ratio of the source emf E to the cut-in voltage U_0 of the diode, if the charge passed through the diode after the switch was opened is n times greater than the charge passed through the inductor during the period t_0 when the switch was closed.



Problem 3

In this problem, the motion of a uniform rod (stick) with length L , ended with caster-wheels at both ends, will be investigated on a horizontal surface. The casters at each end of the rod can spin freely and independently (see Figure 1) and have a negligible mass compared to the rod. The friction between the rod and the caster-wheels is negligible. The diameter of the caster-wheels are a bit larger than the diameter of the rod, but both diameters are much smaller than the length of the rod. The gravitational acceleration is g .



Figure 1: Sketch of the rod with the caster-wheels.

1. The rod is placed on a horizontal surface and pushed such that each end of the rod get different horizontal initial velocity (v_1 and v_2 , pointing in the same direction) perpendicular to the axis of the rod. The casters roll without slipping on the surface.

- Calculate the initial velocity v_0 of the center of the rod and the initial angular velocity ω_0 of the rod using v_1 , v_2 and L ! (0.8 points)
- Describe the motion of the center of mass of the rod! Determine the parameter(s) of its orbit!

(0.8 points)

(c) What should be the minimum value of the coefficient of static friction μ for the casters to not slip on the surface? (0.6 points)

In the following sections the case of the inclined surface will be considered. The angle between the inclined surface and the horizontal plane is α .

2. If α is infinitesimally small, the motion of the rod slightly changes: the motion of the center of mass is approximately the same as in the previous section but a constant drift velocity v_{drift} added to the solution. Use a coordinate system as in Figure 2.

(a) Calculate the magnitude and the direction of v_{drift} as a function of the small α , the initial velocities of the two ends of the rod (v_1 and v_2 , pointing in the same direction) and the gravitational acceleration g !

(1.9 points)

(b) Sketch the orbit of the center of mass of the rod! (0.5 points)

3. If α is finite, the details of the motion of the rod changes. Place the rod on the inclined plane along the steepest line of the surface (so the rod is parallel with the inclined edges of the plane). Consider that the initial velocity v_0 of the center of mass of the rod is perpendicular to the axis of the rod and the initial angular velocity ω_0 is perpendicular to the surface as shown in Figure 2.

(a) Calculate the time evolution of the velocity $v(t) = (v_x(t); v_y(t))$ of the center of mass of the rod in the Cartesian coordinate system shown in Figure 2. (0.8 points)

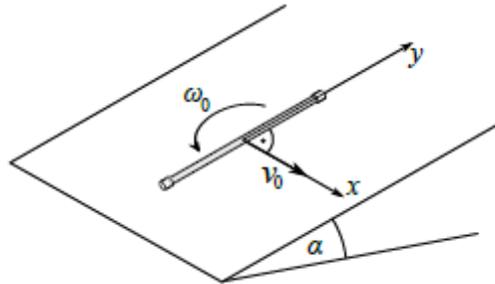


Figure 2: The initial conditions of the rod in section 3.

(b) Depending on the magnitude of the v_0 and ω_0 , it can occur, that the center of the rod stops for a moment during its motion. Express the condition(s) for such a behavior using the parameters v_0 , ω_0 , g , α and L ! (0.8 points)

(c) Determine the maximum displacement of the center of the rod in the direction of the steepest line (y -direction) as function of v_0 and ω_0 ! (1.2 points)

4. Investigate another situation where the rod is placed horizontally on the inclined surface. Consider that the initial angular velocity ω_0 of the rod is perpendicular to the surface but the initial velocity of the center of the rod is zero (see Figure 3).

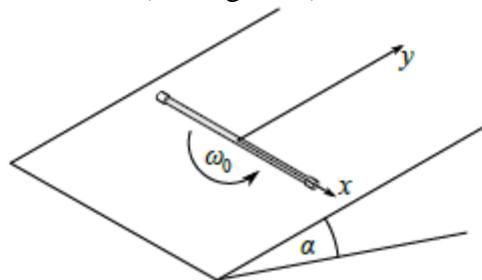


Figure 3: The initial conditions of the rod in section 4.

(a) Describe the motion of the center of mass of the rod! Determine the parameter(s) of its orbit! (1.6 points)

(b) What should be the minimum value of the coefficient of static friction μ in this case for the casters to not slip on the surface? (1.0 points)

Experimental Problem¹

WIND POWER AND ITS METROLOGIES

I. APPARATUS

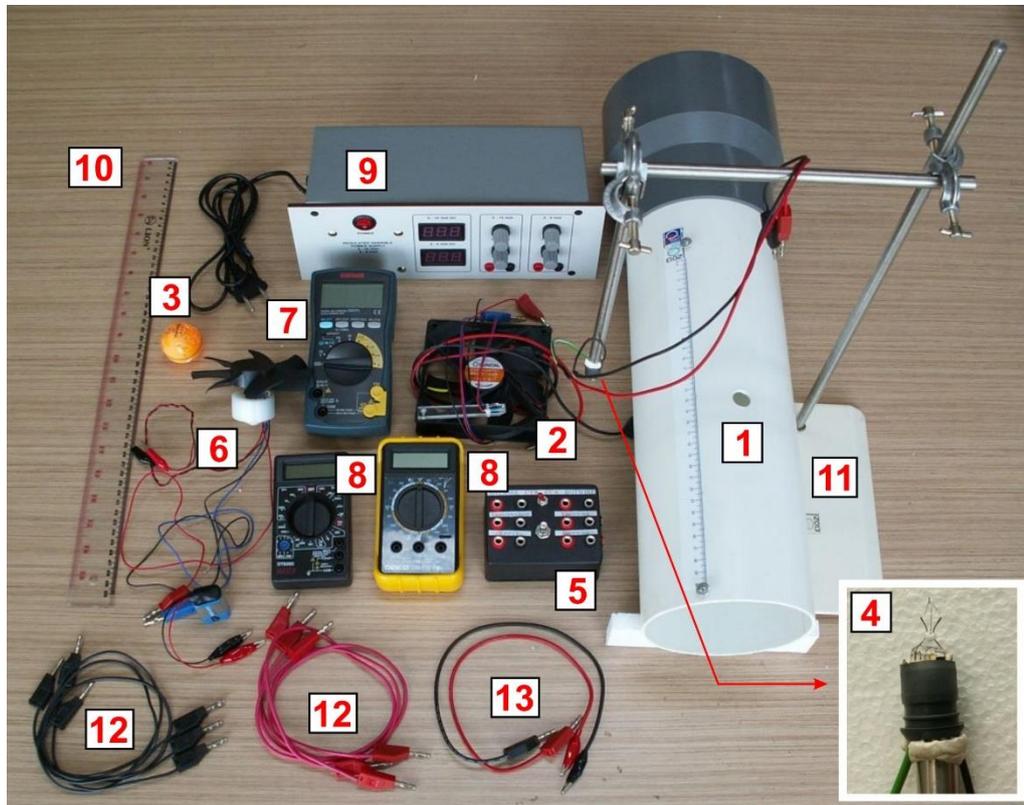


Figure 1. Overall setup

1. Wind tunnel with nichrom (nickel-chromium) wire
2. Computer fan: with frequency sensor
3. Ping pong ball
4. Hotwire filament: **Please be careful not to touch the filament**
5. Electronic box for hotwire
6. Turbine: with frequency sensor
7. Digital MultiMeter (DMM) #1: for frequency measurement
8. DMM#2 and #3
9. Power Supply: with adjustable output 15 V max and 9 V max
10. Ruler (50 cm)
11. Static stand
12. Cables with banana jacks on both ends (3 pairs)
13. Cable with banana jack and crocodile jack on each end (1 pair)

CONSTANTS & DATA:

Gravitational acceleration	:	$g = 9.81 \text{ m/s}^2$
Mass density of air	:	$\rho_A = 1.2 \text{ kg/m}^3$

¹ Experimental Problem of World Physics Olympiad.

Ping pong ball diameter	:	$d_B = (39.5 \pm 0.1) \text{ mm}$
-------------------------	---	-----------------------------------

II. INTRODUCTION

Wind power is a rapidly expanding source of renewable and clean energy and is becoming more important to power our growing population. The wind power can be converted to useful electrical power using wind turbine as shown in Figure 1.

We will explore the physics of wind power and wind turbine and their related metrologies. We will investigate two methods of measuring wind speed i.e. ping pong ball anemometer and hot wire anemometer. Finally we will also explore the physics of wind turbine and its power conversion efficiency. We will use a wind tunnel with a suction fan on one end that provides a laminar (not turbulent) wind flow.²

This experiment is divided into five sections:

- A. Theoretical background
- B. The wind tunnel
- C. Ping pong ball anemometer
- D. Hot wire anemometer:
 - (1) Constant Temperature Method
 - (2) Constant Current Method
- E. Wind turbine



Figure 2. An array of wind turbine in a wind farm

III. EXPERIMENT & QUESTIONS

[A] Theoretical Background [1.3 pt]

We will explore basic theoretical aspects of wind power and power conversion efficiency of a wind turbine.

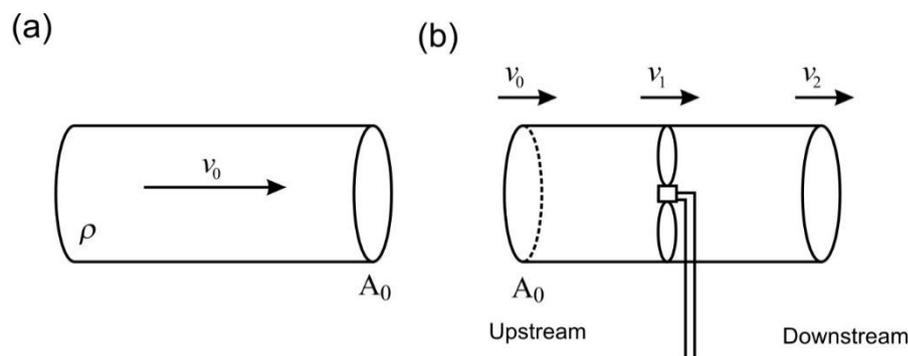


Figure 3. (a) A tubular packet of wind (b) A wind turbine intercepting the wind flow

[A.1] Consider a packet of air with mass density ρ_A flowing through a tube with a cross section area A as shown in Figure 3(a). Show that the power contained in the wind is:

² In contrast, a wind tunnel with a fan blowing into the tunnel has more turbulent wind flow

$$P_W = \frac{1}{2} \rho_A A v_0^n. \quad (1)$$

What is the value of n ? We will also determine n experimentally in part B.3.

[0.4 pt]

[A.2] Now consider a wind turbine with a rotor area A_0 , intercepting a tubular section of the wind of the same cross section area as shown in Figure 3(b). The upstream and downstream wind velocities are v_0 and v_2 . Assume that the velocity at the rotor is the average *i.e.* $v_1 = (v_0 + v_2)/2$. Show that the maximum power that can be extracted by the wind turbine can be written as :

$$P_R = \beta \rho_A A_0 (v_0 + v_2)(v_0^2 - v_2^2) \quad (2)$$

What is β ?

[0.3 pt]

[A.3] The downstream wind slows down by a factor λ , where $\lambda = v_2 / v_0$. For the turbine to extract maximum power, λ cannot be too low (as the wind flow will stop) or too high (which means the turbine captures very little power from the wind). Find the optimum value of λ that will yield the maximum power for the wind turbine.

[0.4 pt]

[A.4] We define rotor efficiency (or power coefficient) C_p as the power that can be extracted by rotor of the wind turbine P_R over the available wind power P_W :

$$C_p = \frac{P_R}{P_W}. \quad (3)$$

Based on your answer in question A.3, find the maximum value of C_p . This value is called Betz efficiency³ which sets the theoretical limit of maximum power conversion efficiency of a wind turbine.

[0.2 pt]

[B] The Wind Tunnel [3.0 pt]

We will use a wind tunnel with a computer fan to serve as *wind generator* by blowing the wind out of wind tunnel (a suction type wind tunnel)¹ to achieve a more laminar flow of wind.

Measuring the rotation speed of the motor or wind turbine is important in wind power engineering. We will use a simple optoelectronic-sensor circuit as shown below to measure the rotation frequency of the motor. The opto-sensor consists of a pair of infrared light emitter and detector that will detect a reflective strip on the motor as the motor rotates (Figure 4).

INSTRUCTION & WARNINGS:

- (a) Connect the opto-sensor circuit as shown in Figure 4.
- (b) **WARNING: Please be careful with the crocodile jacks on the battery for the opto-sensor, they are quite fragile.**
- (c) **WARNING: If you don't need to read the motor frequency please disconnect the battery to avoid draining its power.**

³ Albert Betz, a German physicist who derived this formula in 1919.

- (d) **WARNING:** If you need to read the voltage from the power supply, you can use DMM (digital multimeter) to get more significant figures.
- (e) **WARNING:** If you are using the DMM as an ampere-meter beware of the range limit. If you blow the DMM fuse only one replacement is provided.

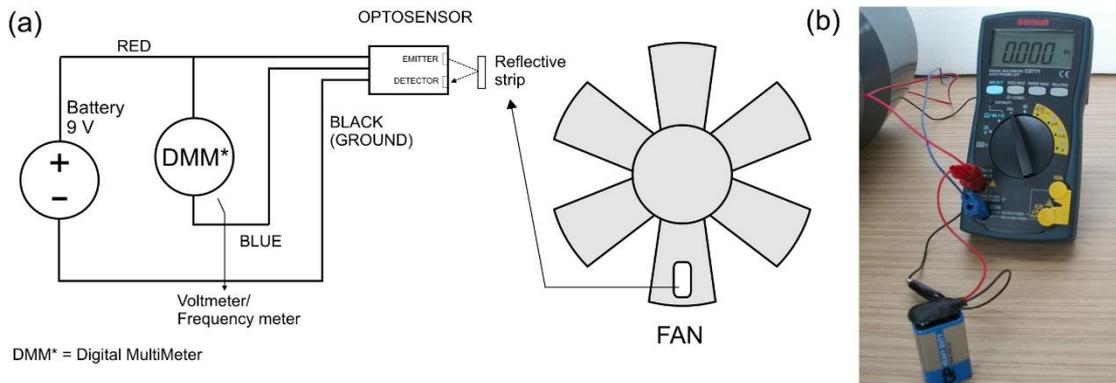


Figure 4. Opto-sensor output connection to the DMM#1 that works as voltmeter or frequency meter.

[B.1] With no power to the motor, switch DMM#1 to voltmeter mode (labeled **V** on the DMM) and rotate the fan manually and slowly and you will see the voltage is changing. Plot the opto-sensor's signal as a function of blade rotation (or time). Indicate the period of the signal. [0.7 pt]

The wind speed inside the tunnel is mainly determined by the rotation frequency (f_M) of the wind generator motor. The relationship between the wind speed (measured at the center of the tunnel) and the motor frequency has been measured as shown in Figure 5 below and follows a simple linear relationship:

$$v = (0.0873 \pm 0.0012) \text{ meter} \times f_M \quad (4)$$

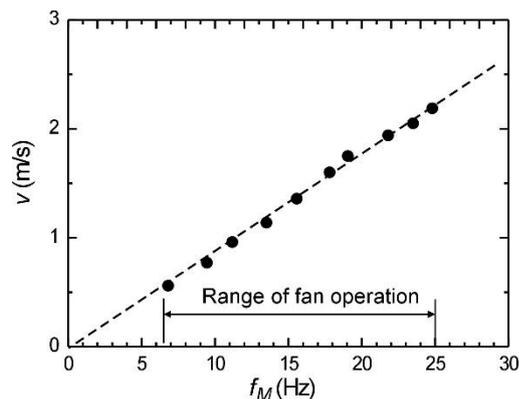


Figure 5. Wind velocity (at the center of the tunnel) vs. the motor fan rotation frequency.

[B.2] The motor fan has fairly fixed mechanical efficiency (ratio of the wind power P_W generated over the input electrical power to the motor fan P_M) for the rated voltage: $3 \text{ V} < V_M < 12 \text{ V}$. This mechanical efficiency is given by $\eta_M = P_W / P_M$. Perform an experiment to determine the mechanical efficiency η_M and the power factor n for the wind power P_W in Eq. 1. Sketch your connection diagram.

[2.4 pt]

[C] Ping Pong Ball Anemometer [3.5 pt]

Measuring wind speed is a primary metrology activity in wind power engineering. We will investigate a very simple method to measure wind speed using a ping pong ball pendulum as shown in Figure 6.

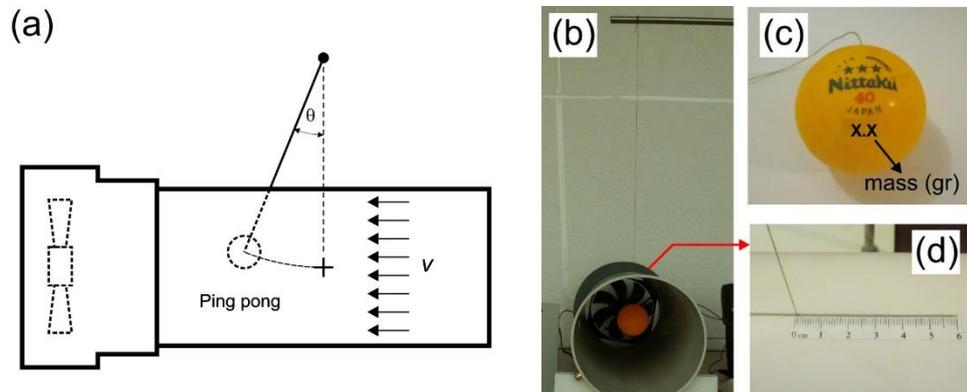


Figure 6. Ping pong ball anemometer experiment

The principle of operation is very simple, the wind will impose a drag force and deflect the ping pong pendulum by an angle θ . This drag force is given by:

$$F_D = \frac{1}{2} C_D \rho_A A_B v^m, \quad (5)$$

where C_D is the drag coefficient of the object, ρ_A is the density of the fluid (air), A_B is the cross section of the ping pong ball, v is the velocity of the ball relative to the fluid and m is the power factor. Mass of the ping pong ball m_B (in gram) is written on the ball as shown Figure 6(c). Please refer to **Constants & Data** in. pg. 2 for other data.

INSTRUCTIONS & WARNING:

- (a) Insert the pendulum thread into the slot with the imprinted ruler as shown in Figure 6(d). Position the ping pong ball at the center of the tunnel. The imprinted ruler helps you to calculate the deflection angle θ
- (b) **WARNING:** The joint between the thread and the ping pong ball is fragile. Please be gentle.
- (c) **WARNING:** Please make sure that the thread is free to move, not sticking to the slot. You can verify this by making sure that after the pendulum is deflected by the wind it can go back to the original rest position when there is no wind. You can nudge or push a little bit the pendulum thread with a pen to make sure that the thread does not get stuck.
- (d) **WARNING:** If you do not need to read the motor frequency, please disconnect the 9V battery to avoid draining its power.

[C.1] Develop a model that relates the wind speed v as a function of the deflection angle θ . Express your answer in terms of, among others, mass density of the air (ρ_A) and the ping pong ball mass (m_B).

[C.2] Perform an experiment to determine C_D and m .

[D] Hot Wire Anemometer [5.8 pt]

The ping pong ball anemometer we studied just now is not really suitable for practical applications that usually requires electrical read-out. Thus, we will investigate another method of measuring wind speed: hot-wire anemometer (HWA). HWA utilizes a filament that becomes hot as electrical current is passed through it. As the wind blows, it introduces forced convection that takes away heat from the filament so the temperature (and thus the resistance) of the filament will drop as shown in Figure 7 (unless compensated by increasing the electrical power). This phenomenon can be exploited to measure the wind speed. In this experiment we will study the characteristics of the hot wire with respect to varying wind velocity.

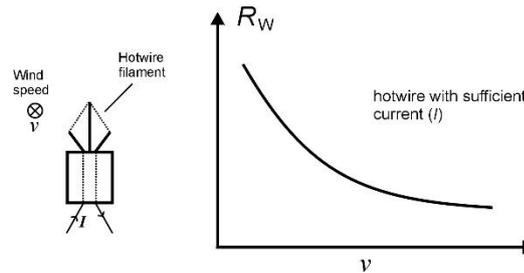


Figure 7. Hot wire anemometer with wind blowing into the plane

We use a metal (tungsten) filament from an ordinary light bulb where the bulb is intentionally broken to expose the filament. For a small change of temperature, the filament resistance follows a linear relationship:

$$R_w = R_0[1 + \alpha(T_w - T_0)], \quad (6)$$

where R_w is the filament's resistance at temperature T_w , R_0 is the resistance at temperature T_0 and α is the temperature coefficient of the resistance. For tungsten, the value is $\alpha = 4.5 \times 10^{-3} / ^\circ\text{C}$.

Now, we will consider the heat transfer between the filament and its surrounding, which can happen through natural convection (without external source of wind/fluid movement), forced convection (with external source of disturbance), conduction (mainly to the filament's holder and base) and radiation.

Consider the case where the filament is heated by external power such as by electric current, and is transferring the heat to its surrounding by all the processes above. After the system has reached equilibrium, the power balance can be expressed as:

$$P_{\text{input}} = Q_{\text{forced convection}} + Q_{\text{natural convection}} + Q_{\text{conduction}} + Q_{\text{radiation}},$$

$$V \cdot I = h' A_w (T_w - T_0) + Q_{\text{nc}} + Q_{\text{conduction}} + A_w \sigma \epsilon (T_w^4 - T_0^4), \quad (7)$$

where A_w is the surface area of the filament, T_0 the room/surrounding temperature (presumably the original temperature of the filament), σ the Stefan-Boltzmann constant, ϵ the emissivity and h' the forced convection heat transfer coefficient.

For the forced convection of the hot wire filament, the forced convection process can be expressed as King's law: $h' = a' + b v^c$, where a' and b are constants and c is the power factor of the wind velocity. The filament's length is much larger than its width hence the heat transfer by means of

conduction can be ignored. For small temperature difference ($T_w \sim T_0$), $T_w^4 - T_0^4 \sim T_0^3(T_w - T_0)$, so the radiation heat transfer can be written as $3A_w\sigma T_0^3(T_w - T_0) \rightarrow k(T_w - T_0)$ and Q_{nc} can be considered constant. After taking into account all these we can rewrite Eq. (7) as:

$$V_w \cdot I_w = (a + bv^c)A_w(T_w - T_0), \quad (8)$$

with $a = a' + Q_{nc}/(T_w - T_0) + 3A_w\sigma T_0^3$.

Now we will perform experiments to determine the value of b/a and c with two different methods: hotwire with constant temperature and with constant current flowing through it.

Mount the hotwire filament to a steel rod as shown in Figure 8(a) and put it inside the wind tunnel through the hole (you can rotate the wind tunnel). When you insert the hotwire into the wind tunnel, make sure you have correct orientation: the largest cross section of the hotwire filament is perpendicular to the wind flow, see Figure 8(b).

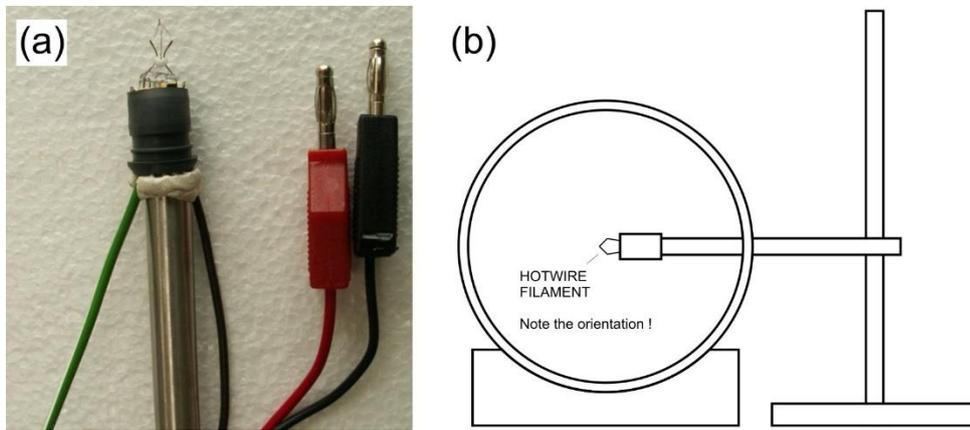


Figure 8. (a) Hotwire filament (b) Hotwire filament in the wind tunnel

The two experiments require some electronic circuit to perform which we provide in an electronic box, see Figure 9 below. To perform each of the experiment, you will only need one side of the circuit. There is a small switch on the top of the box to toggle between the two, labeled as CTA (Constant Temperature Anemometer) and CCA (Constant Current Anemometer).

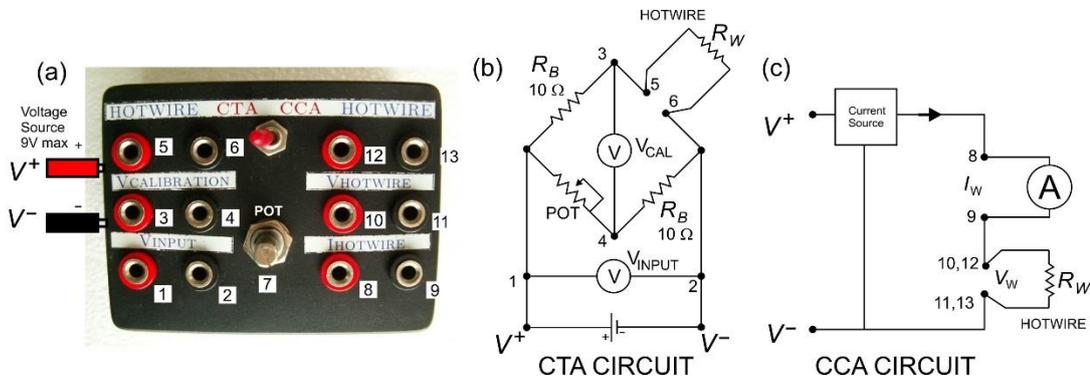


Figure 9. (a) Hotwire electronic box (b) Constant Temperature Anemometer (CTA) circuit (c) Constant Current Anemometer circuit (CCA).

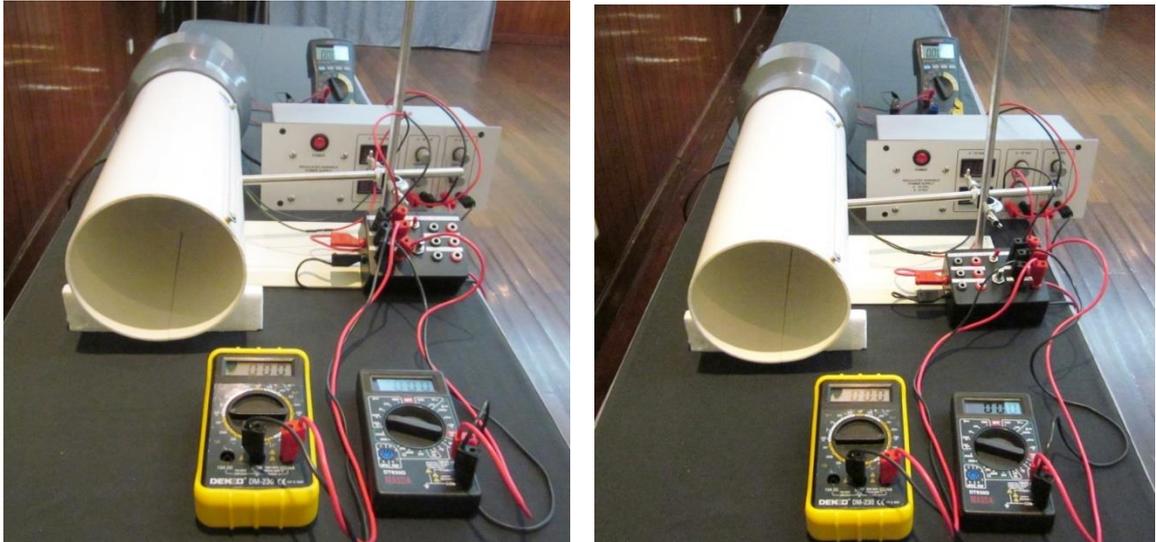


Figure 10. (a) Constant temperature anemometer (CTA) setup. (b) Constant current anemometer (CCA) setup.

[D.1] Constant Temperature Method [2.7 pts]

The constant temperature method is performed by keeping the temperature of the hotwire (and thus its resistance) constant for different wind speed. To achieve this we use Wheatstone bridge with a variable (POT) resistor across the hotwire to balance the bridge as shown in Figure 9(a).

First we balance the bridge by tuning the potentiometer (POT) to set the $V_{CALIBRATION}$ to zero. When the wind speed increases, R_w reduces and the bridge goes out of balance. To restore R_w and rebalance the bridge we need to increase V_w (or V_{INPUT}) to increase power dissipation.

The following formula is used in the constant temperature experiment:

$$\frac{V_w^2}{R_w} = (a + bv^c) A_w (T_w - T_0), \quad (9)$$

with V_w and R_w are potential and resistance across the hotwire. We do not measure the hotwire potential, instead we measure the potential drop through the Wheatstone bridge (V_{INPUT}). With this substitution, Eq. 9 above can be rewritten as:

$$V_{INPUT}^2 = A + Bv^c. \quad (10)$$

[D.1.1] What is A and B ?

[0.4 pt]

Eq. 10 can be rewritten into a linear form that you can use in linear regression:

$$\log y = \log \frac{b}{a} + c \log v. \quad (11)$$

[D.1.2] What is y ?

[0.3 pt]

[D.1.3] Perform the experiment and obtain b/a and c !

[2.0 pt]

INSTRUCTIONS & WARNING:

- (a) Switch the electronics box to constant temperature (CTA) mode.
- (b) Connect the wires and jacks according to **Ошибка! Источник ссылки не найден.** above. Use the 9V power source for the hotwire electronic box.
- (c) **WARNING: Please be careful not to touch and damage the hotwire filament.** If you damage the hotwire, you will be provided with **only 1 replacement hotwire during the whole experiment.**
- (d) **Carefully inspect** that you have all **the connections correct** and make sure **all the knobs** on the power supply are **turned all the way down (left)** before you turn it on.
- (e) Turn on the power supply and slowly increase the voltage to the electronic box to around 1 V. After this, you have to adjust the potentiometer on the Wheatstone bridge so that V_{CALIB} is zero. Before the wind is blowing, adjust the potentiometer so that V_{CALIB} is zero. We called the bridge in this condition balanced.
- (f) **WARNING: do not use voltage higher than 2 V when there is no wind, you may damage the hotwire.** The hotwire is damaged if it glows. Remember: **only 1 replacement hotwire is allowed for the whole experiment.**
- (g) Increase wind speed, adjust V_{INPUT} so that the bridge is balanced again, *i.e.* the hotwire resistance has returned to the initial value.
- (h) Repeat step (g) until you have enough data. Record your data on the answer sheet and plot your graph to determine b/a and c .
- (i) **WARNING: Do not turn down the power to the motor before you turn off the power to the hotwire.** If you do, the hotwire will overheat and may be damaged. Remember: **only 1 replacement hotwire is allowed for the whole experiment.**

[D.2] Constant Current Method [3.1 pts]

The constant current experiment is done by keeping the current through the hotwire constant using the electronic box that serves as constant current source. The current can be adjusted by tuning the potentiometer on the box.

The following formula is used for constant current experiment:

$$V_w \cdot I_w = (a + bv^c) \frac{A_w}{\alpha R_0} (R_w - R_0), \quad (12)$$

which is obtained from Eq. 8 with the following substitution: $T_w - T_0 = \frac{R_w - R_0}{\alpha R_0}$.

In this experiment, we first need to measure R_0 , which is done when there is no wind ($v=0$). Eq. (12) can be rewritten as:

$$\frac{V_w}{I_w} = \frac{R_0}{k} V_w \cdot I_w + R_0. \quad (13)$$

[D.2.1] What is k ?

[0.2 pt]

[D.2.2] Perform an experiment to determine the value of R_0 .

[1 pt]

INSTRUCTION & WARNINGS:

- (a) Switch the electronics box to constant current (CCA) mode.
- (b) Connect the wires and jacks according to Figure 9(b) and Figure 10(b). **Carefully inspect that they are correct and** make sure **all the knobs on the power supply are turned all the way down (left)** before you turn it on.
- (c) Turn on the power supply and slowly increase the voltage or current to the hotwire.
- (d) **WARNING: do not use current higher than 180 mA, you may damage the hotwire.** The hotwire is damaged if it glows. Remember: **only 1 hotwire replacement is allowed.**
- (e) Notice that you can limit the current to the hotwire by adjusting the potentiometer on the box (*i.e.* the current and voltage across the hotwire will not increase even when you increase the voltage on the power supply). We suggest you to **set the voltage** from power supply **to 7.5 V** to have a **stable working voltage** for the **electronics box**.
- (f) **Make sure the DMM** to measure the current **is working properly**, *i.e.* the **reading is not zero**. The current measurement circuit on a DMM is protected by a fuse. If the fuse is broken, the DMM will still appear to be working but the current measurement will always be zero.
- (g) Record the current and voltage across the hotwire.
- (h) Repeat step (g) until you have enough data. Record your data on the answer sheet and plot your graph to determine k and R_0 .

Now we are ready to determine b/a and c like in the constant temperature case. Rewrite Eq. 12 into the following form:

$$\log y = \log \frac{b}{a} + c \log v. \quad (14)$$

[D.2.3] What is y in this case?

[0.2 pt]

[D.2.4] Perform an experiment to determine b/a and c .

[1.7 pt]

INSTRUCTIONS & WARNINGS:

- (a) **Make sure all the knobs on the power supply are turned all the way down (left)** before you turn it on. Turn on the power supply and slowly increase the voltage/current to the hotwire.

- (b) Adjust the potentiometer to the working current that you desire.
Warning: do not use current higher than 180 mA, you may damage the hotwire. The hotwire is damaged if it glows. Remember: **only 1 hotwire replacement is allowed.**
- (c) Turn up the motor wind generator voltage to generate wind.
- (d) Record the current and voltage across the hotwire for this wind speed.
- (e) Readjust the wind speed and repeat step (d) until you have enough data.
- (f) Record your data on the answer sheet and plot your graph to determine b/a and c .

[E] Wind Turbine [6.3 pt]

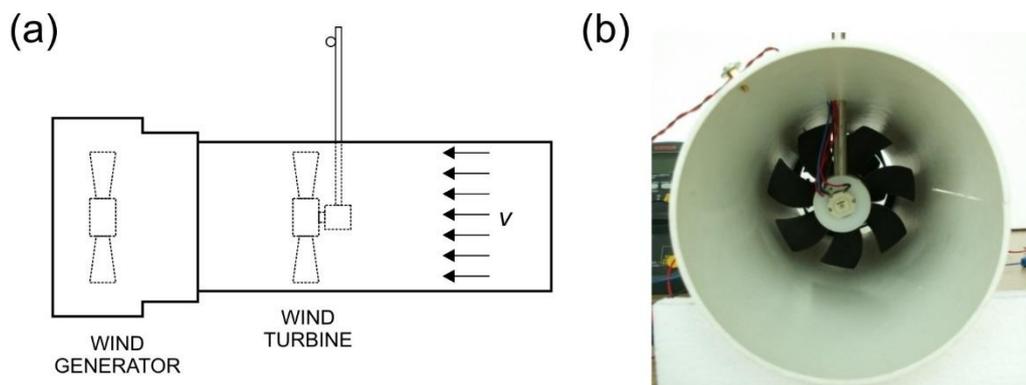


Figure 11. The wind turbine experiment setup

We will explore the physics of wind turbine and investigate its power conversion efficiency. In this experiment we use a simple DC motor to serve as a wind turbine that converts the mechanical power from the rotor into electrical power.

One factor that determines the efficiency of a wind turbine is the external load. In this experiment, we will investigate the load that generates maximum efficiency for a wind turbine, by using a resistive nickel-chromium (nichrom) wire to simulate a low resistive load ($< 2 \text{ ohm}$). This load can be changed by varying the length of the wire. Use the crocodile clips to contact the wire.

One key parameter that influence the wind turbine efficiency is Tip Speed Ratio (TSR), which is defined as:

$$TSR = \frac{\Omega R}{v}, \quad (15)$$

where Ω the angular speed of the blade, R the radius of the turbine rotor blade and v the wind speed coming on the rotor at the tip of the blade. We assume the wind speed is uniform across the cross section of the tunnel.

The motor turbine has an equivalent internal circuit as shown below. A rotating coil provides electromotive force (emf) voltage when the motor rotates and an effective series resistance R_M , which is the sum of resistance of the rotor coil inside the motor. R_M is small but not negligible ($< 2 \Omega$). Thus the real motor can be modeled as an ideal motor (whose coil has no resistance) plus a series resistance R_M as shown below.

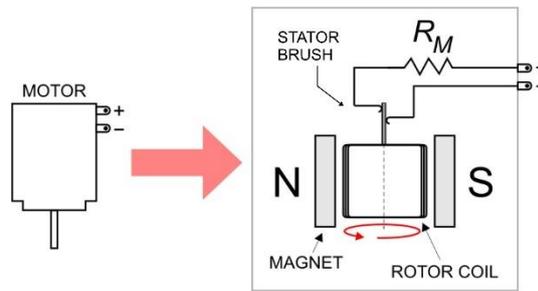


Figure 12. The equivalent circuit of the motor (wind turbine)

[E.1] Determine the internal series resistance of the motor turbine R_M . Note that the moving contact between the rotor and stator brush of the DC motor (see Figure 12) may add extra resistance that may vary with the position of the turbine blade.

[0.6 pt]

[E.2] Determine the resistance per unit length of the nichrom wire, λ_R (in Ω/m). Note that the range of resistance of nichrom wire is low (< 7 ohm) comparable to the cable resistance of the digital multimeter (DMM).

[1.2 pt]

If you need constant current source you can use the hotwire electronic box in Constant Current Anemometer (CCA) mode. **If you need to use amperemeter use DMM#2 or #3 and please be careful not to exceed the rating or to blow the fuse.**

INSTRUCTIONS:

- (a) Place the turbine inside the wind tunnel. First, route the banana and crocodile jacks of the turbine through the small hole on the top of the wind tunnel from inside the tunnel. Then insert the mounted steel rod (use the one for hotwire) into the hole and put the turbine at the end of it, see **Ошибка! Источник ссылки не найден.** below.
- (b) You will need to measure two frequencies in this experiment: the wind generator frequency (to obtain the wind speed) and the wind turbine frequency. You can do this by combining the connection as shown in Figure 13(a).
- (c) Connect the nichrom wire as load to the motor turbine using crocodile clips. You can measure the voltage across the wire section *separately* by simply connecting the voltmeter at both ends of the nichrom wire as shown in Figure 13(b).

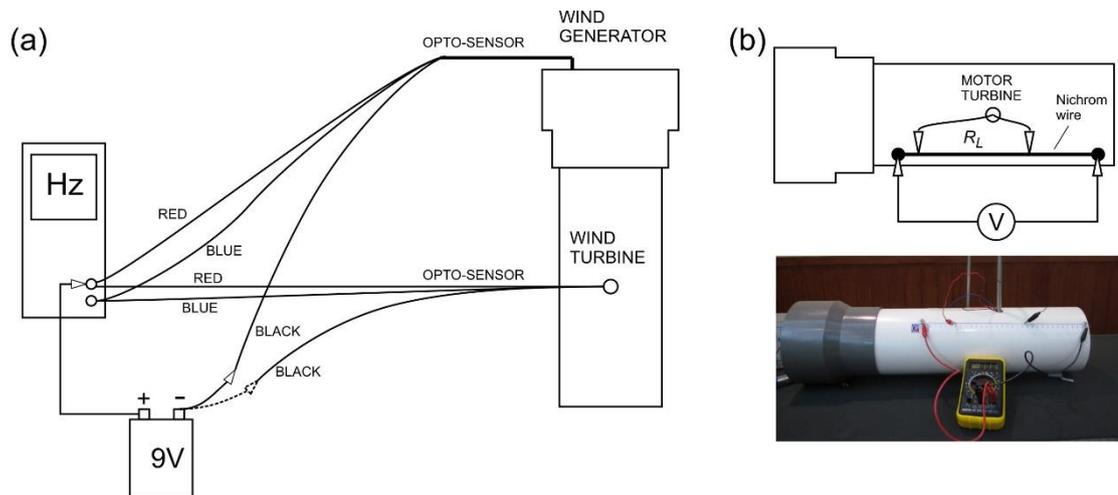


Figure 13(a) Connection to read two frequencies. Select the black wire to switch between reading wind generator or wind turbine. (b) Connection to the nichrom wire as a load. Note that the Voltmeter is connected at both ends of the nichrom wire.

[E.3] Perform experiment to determine the optimum load R_L for maximum power transfer. Plot the power delivered to R_L vs. R_L or nichrom length l . What do you expect theoretically for R_L ? [2.9 pt]

The wind turbine efficiency η_{WT} is defined as the ratio of power delivered to the load R_L to the available wind power P_W .

[E.4] Using the optimum load R_L that you found experimentally in E.3, plot η_{WT} vs. TSR. [1.6 pt]